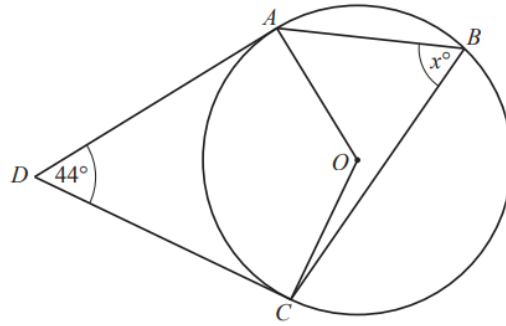


IGCSE PAST  
PAPER 2  
(0580)  
EXTENDED

CIRCLE THEORME

WRITTEN BY RISHI

1



NOT TO  
SCALE

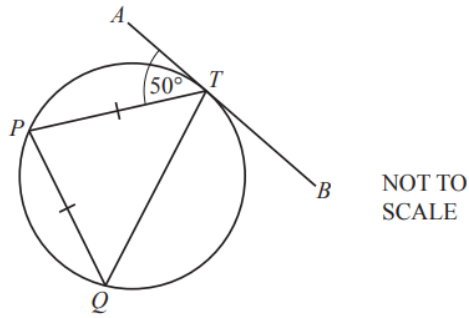
*A, B and C are points on a circle, centre *O*.*  
*DA and DC are tangents.*  
*Angle  $ADC = 44^\circ$ .*

Work out the value of *x*.

$x = \dots\dots\dots$  [3]

0580/22/M/J/21

(a)



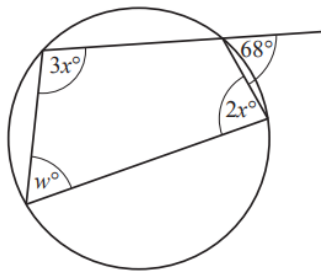
NOT TO SCALE

$P, Q$  and  $T$  are points on a circle.  
 $ATB$  is a tangent to the circle at  $T$  and  $PT = PQ$ .

Find angle  $TPQ$ .

Angle  $TPQ = \dots\dots\dots$  [2]

(b)



NOT TO SCALE

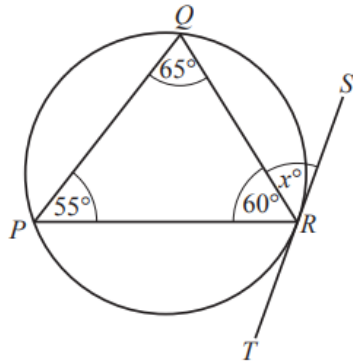
The diagram shows a cyclic quadrilateral with an exterior angle of  $68^\circ$ .

Find the value of  $w$  and the value of  $x$ .

$w = \dots\dots\dots$

$x = \dots\dots\dots$  [3]

3



NOT TO SCALE

$P$ ,  $Q$  and  $R$  are points on a circle.  
 $ST$  is a tangent to the circle at  $R$ .

- (a) Write down the value of  $x$ .  
Give a geometrical reason for your answer.

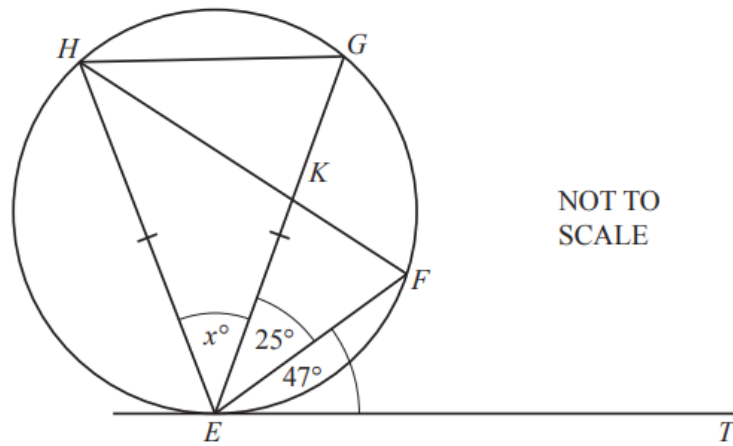
$x = \dots\dots\dots$  because  $\dots\dots\dots$   
 $\dots\dots\dots$  [2]

- (b) Another tangent from the point  $S$  touches the circle at  $V$ .

Give a geometrical reason why triangle  $SVR$  is isosceles.

$\dots\dots\dots$   
 $\dots\dots\dots$  [1]

4



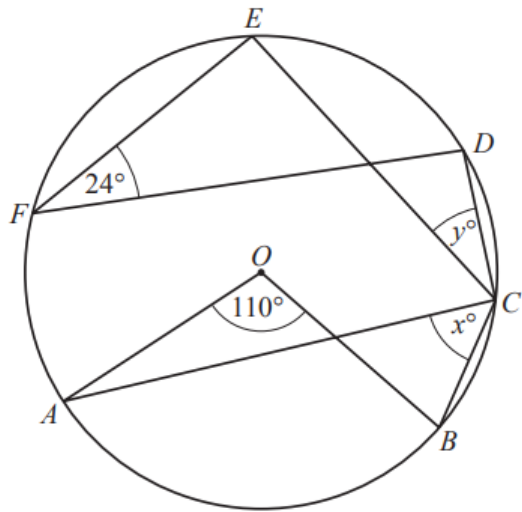
NOT TO SCALE

Points  $E, F, G$  and  $H$  lie on the circle and  $EG = EH$ .  
 $HF$  and  $EG$  intersect at  $K$ .  
 $ET$  is a tangent to the circle at  $E$ .  
Angle  $FET = 47^\circ$  and angle  $FEG = 25^\circ$ .

Find the value of  $x$ .

$x = \dots\dots\dots$  [2]

0580/22/F/M/21



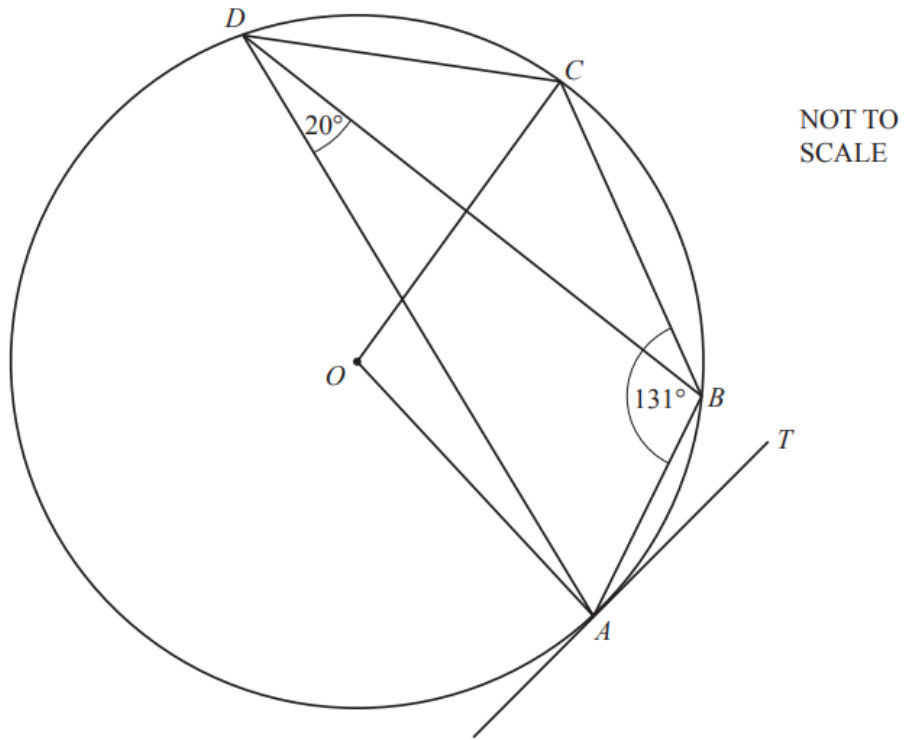
NOT TO SCALE

Points  $A, B, C, D, E$  and  $F$  lie on the circle, centre  $O$ .

Find the value of  $x$  and the value of  $y$ .

$x = \dots\dots\dots$

$y = \dots\dots\dots$  [2]



$A, B, C$  and  $D$  lie on the circle, centre  $O$ .  
 $TA$  is a tangent to the circle at  $A$ .  
 Angle  $ABC = 131^\circ$  and angle  $ADB = 20^\circ$ .

Find

(a) angle  $ADC$ ,

Angle  $ADC = \dots\dots\dots$  [1]

(b) angle  $AOC$ ,

Angle  $AOC = \dots\dots\dots$  [1]

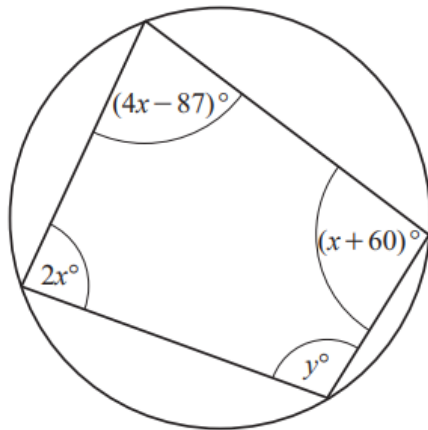
(c) angle  $BAT$ ,

Angle  $BAT = \dots\dots\dots$  [1]

(d) angle  $OAB$ .

Angle  $OAB = \dots\dots\dots$  [1]

7



NOT TO  
SCALE

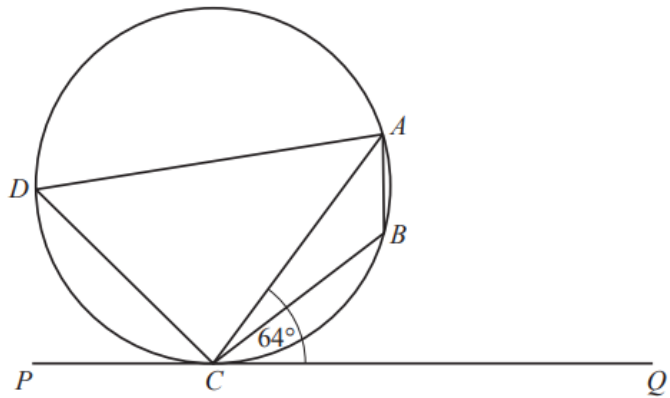
The diagram shows a cyclic quadrilateral.

Find the value of  $y$ .

$y = \dots\dots\dots$  [4]

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8



NOT TO SCALE

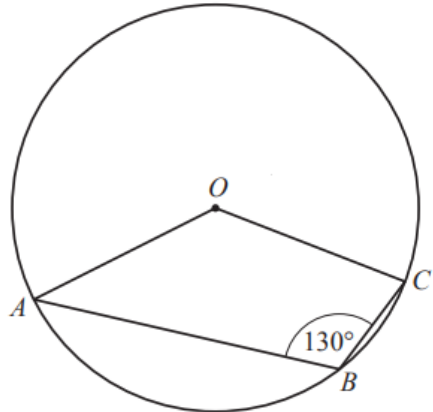
$A, B, C$  and  $D$  lie on the circle.  
 $PCQ$  is a tangent to the circle at  $C$ .  
 Angle  $ACQ = 64^\circ$ .

Work out angle  $ABC$ , giving reasons for your answer.

Angle  $ABC = \dots\dots\dots$  because  $\dots\dots\dots$   
 $\dots\dots\dots$   
 $\dots\dots\dots$  [3]

0580/22/F/M/20

9



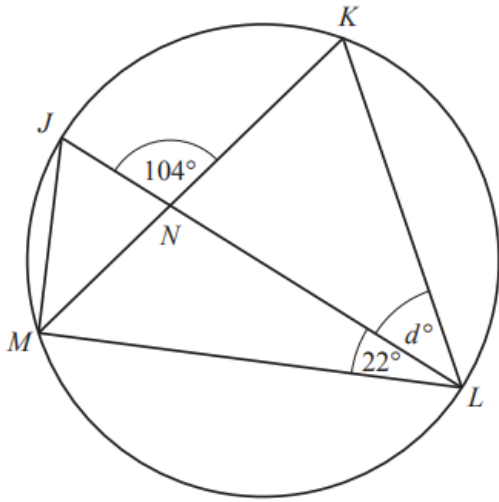
NOT TO SCALE

$A, B$  and  $C$  are points on the circle, centre  $O$ .  
 Find the obtuse angle  $AOC$ .

Angle  $AOC = \dots\dots\dots$  [2]

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10



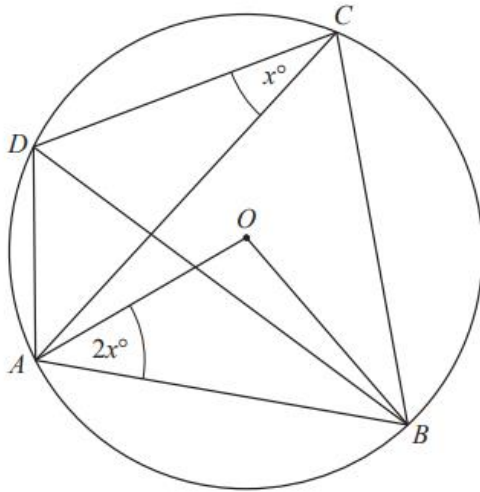
NOT TO  
SCALE

$J, K, L$  and  $M$  are points on the circumference of a circle with diameter  $JL$ .  
 $JL$  and  $KM$  intersect at  $N$ .  
Angle  $JNK = 104^\circ$  and angle  $MLJ = 22^\circ$ .

Work out the value of  $d$ .

$d = \dots\dots\dots$  [4]

0580/23/M/J/19



NOT TO SCALE

In the diagram,  $A, B, C$  and  $D$  lie on the circumference of a circle, centre  $O$ .  
 Angle  $ACD = x^\circ$  and angle  $OAB = 2x^\circ$ .

Find an expression, in terms of  $x$ , in its simplest form for

(a) angle  $AOB$ ,

Angle  $AOB = \dots\dots\dots$  [1]

(b) angle  $ACB$ ,

Angle  $ACB = \dots\dots\dots$  [1]

(c) angle  $DAB$ .

Angle  $DAB = \dots\dots\dots$  [2]